

THE POYNTING-ROBERTSON EFFECT ON METEOR ORBITS

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流星、軌道 = 対スル ポインティング-ロバートソン 効果

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ABSTRACT

The Poynting-Robertson effect will operate to sweep small particles of the solar system into the sun at a cosmically rapid rate. Robertson derived an expression for the times of fall from initially circular orbits. Since, if other parameters are equal, the times are much less for orbits of high eccentricity, tables are given here to enable simple calculation of the times of fall in terms of the initial orbital elements, q and e , and particle radius and density. Total times of collapse are computed for several meteor showers.

ポインティング-ロバートソン 効果ハ、太陽系、小ナイ粒子ヲ宇宙中ニ早イ速度デ太陽ニ掃キ落ス作用ヲ行フ。ロバートソンハ、始メ円軌道デアタリ物ノ落下時間、計算式ヲ導イタ。モシ他ノ軌道要素ガ同ジナラバ、太陽近心率ノ軌道デハ、右ト同ク、小ナイデハ、始メ軌道要素ガトビビ粒子ノ半径ト密度ニヨリテ落下時間ヲ簡單ニ計算スルコトガ出来ル事ガ、コニミヘアレイル。イソカノ流星群ニツイテハ、衝突マデノ全時間ガ計算アレイル。

Since there is a linear dependence of the time on particle radius, the material in showers should ultimately be dispersed so that larger particles move with greater orbital a and e than do the smaller ones. This leads to the possibility of observing the Poynting-Robertson effect in a given swarm by a correlation of the observed mean magnitude of meteors with the time while the earth transits the shower. Such a correlation is not detected for any shower definitively; an upper limit, therefore, is set for the age of showers, ranging from five million years for some to less than one hundred thousand years for the Geminids.

If some sporadic meteors had a common origin with the meteorites and asteroids, the operation of the Poynting-Robertson force requires that, for times of origin longer ago than the sixty million years suggested by Bauer, all material of radius less than 0.08 cm has been swept into the sun. Therefore, virtually no sporadic meteors fainter than the fifth magnitude can be arriving now on the earth unless they are cometary or interstellar in origin. For a time of three billion years the minimum radius is about 4 cm.

The tables given for computation of the times of orbital contraction are valid for any radiating body of known mass and radiation by means of a simple correction. The process of contraction is faster by a factor of about 100,000 for B stars than for the sun. But, conversely, the Poynting-Robertson effect due to the general radiation of a galaxy is entirely too small to affect appreciably the dynamics of interstellar dust.

粒子ノ半径ト時間ノ間ニハ、線形(-一次式)ノ関係ガアレイル。流星群ニアル物質ハ、カニ分散スルデ、大ナイ粒子ハ、小ナイモノヨリモ、大キアトビデ動イテイル。コノコカラ、地球ガ流星群ノ中ヲ通過スルキ、流星ノ密度ト関係スル P-R 効果ヲ観測スルコトガ可能ナリ。コノ様ナ関係ガ、ドノ掃キ流星群ニツイテモ必ず見ツカレトハモエナシ。上限ノ値ハ、流星群ノ寿命ニ関係シタリ。例エハ、双子座群ニツイテハ、500万年カヲ数10万年ヲ短イ年数デイル。モシ地球流星ガ隕石ト小惑星ガト同ジ起源ヲ持ツナラバ、P-R 効果ノ影響ハ、Bauerガ示シタルニ、6000万(60 X 100万)年ヲ大キイ寿命ヲ持ツコトナリ、半径ガ 0.08 cm 以下ノ小ナイ物ハ、全テ太陽ニ落チテシタリ。実際ニ、從ッテ、彗星ノ起源カ、2711 恒星間空間ヨリモデナラバ、5等級ヨリ暗イ流星ヲ地球ニ到達スル数ハ流星ノ半径ガ、30億年(英語デハ billion = 10億)ノ寿命ニ対スル最小半径ハ、約 4 cm デイル。

軌道ノ縮小ノ時間ノ計算ハ、与ヘラレタ表ハ、質量ト輻射量ヲ簡單ニ補正スルコトモデテ全テ輻射体ニ適用デキル。縮小ノ過程ハ、B型星ニツイテハ、太陽ヨリ約10万倍モ早イ。コレニ対シ、恒星間空間ノダストノ力学ニ対スル影響ハ、1 輻射ニヨル P-R 効果ハ、カニナクテ3倍ト影響ハナシ。

In the early part of this century, J. H. Poynting¹ considered the effects of the absorption and subsequent re-emission of sunlight by small isolated particles in the solar system. His work was later modified by H. P. Robertson,² who used a precise relativistic treatment to establish, once and for all, the equations of motion for such particles to terms of the first order in the ratio of the velocity of the particle to that of light. While the process of absorption and re-emission produces no net force on a particle when one chooses to work with a stationary frame referred to the particle, it is found when the solar reference frame is used that there is introduced a resisting force on the particle which is proportional to its velocity. The retarding force exhibited in the equations of motion results in a slow secular decrease in semi-major axis and eccentricity of the orbit of any small body. Ultimately the body will fall into the sun.

Robertson が見つけた運動方程式，動径方向の力平衡，成り立つ，

$$\ddot{r} - r\dot{\theta}^2 = -\frac{\mu}{r^2} - \frac{2\alpha\dot{r}}{r^2}, \quad (1)$$

$$\frac{1}{r} \frac{d}{dt}(r^2\dot{\theta}) = -\frac{2\alpha\dot{\theta}}{r^2}, \quad (2)$$

ここで $\mu = GM - \alpha c$ ， α ，外向き方向，輻射 = 32 太陽重力定数，減少量 α は

$$\alpha = \frac{3E_{\odot}}{16\pi c^2 \rho} = \frac{3.79 \times 10^8}{59} \text{ au}^2/\text{year},$$

すなわち

We here denote by E_{\odot} the total energy emitted by the sun per second, for which we have used the value 3.79×10^{33} erg/sec, and by s and ρ the radius and density of the particle in question, expressed in c.g.s. units. It may be noticed at once that equation (2) integrates to

$$H = r^2\dot{\theta} = h - \alpha\theta, \quad (3)$$

where H is the instantaneous value of the angular momentum and h is the initial value.

The secular perturbations for an osculating ellipse of semi-major axis a and eccentricity e have been calculated by Robertson and confirmed by us. For these two elements they are given by

$$\frac{da}{dt} = -\frac{a(2+3e^2)}{a(1-e^2)^{3/2}}, \quad (4)$$

$$\frac{de}{dt} = -\frac{5ae}{2a^2(1-e^2)^{1/2}}. \quad (5)$$

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E_{\odot} は一秒間に放出される太陽の全エネルギーの値 3.79×10^{33} erg/sec である。c.g.s. 単位で表わす微粒子の半径と密度を s と ρ とし、式(2)の両辺を r^2 で乗じ、積分すると $H = r^2\dot{\theta} = h - \alpha\theta$ となる。

$$H = r^2\dot{\theta} = h - \alpha\theta \quad (3) \quad +$$

ここで H は瞬間の角運動量の値で、 h は初期値である。

a と e は永年摂動の Robertson が計算した値である。式(4)と(5)は、軌道要素 a と e の時間変化を示す。

$$\frac{da}{dt} = -\frac{a(2+3e^2)}{a(1-e^2)^{3/2}} \quad (4)$$

$$\frac{de}{dt} = -\frac{5ae}{2a^2(1-e^2)^{1/2}} \quad (5)$$

The only other secular change is the advance of perihelion, which is found by Robertson in the relativistic treatment to be

$$\frac{d\pi}{dt} = \frac{3G^{1/2}M^{1/2}\mu}{c^2 a^{5/2} (1-e^2)}. \quad (6)$$

この永年変化は近日点の前進であり、Robertson の相対論的取り扱いによるものである。

$$\frac{d\pi}{dt} = \frac{3G^{1/2}M^{1/2}\mu}{c^2 a^{5/2} (1-e^2)} \quad (6)$$

* $r^2\dot{\theta} = \text{const.} = \gamma$ である。式(3)を代入すると、(53)の式を得る。

We now seek to find the long-term changes in these elements. It may first be noticed that the expression for perihelion advance is a maximum for large and dense bodies, where $\mu \cong GM$. For the cases in which we are interested, the rate of change is insignificant, amounting, for example, to 43'' per century for Mercury and less than this for small bodies of greater a and smaller e .

Of more interest are the changes in semi-major axis and eccentricity. If we deal with initially circular orbits, equation (4) is simplified and integrates to

$$t = \frac{a^2}{4\alpha} = 7.0 \times 10^4 s \rho a^2 \text{ years,} \quad (7)$$

where t is the total time of fall for a particle of radius s cm, density ρ gm/cm³, at an initial distance of a astronomical units. This formula is due to Robertson. For the more general case of eccentric orbits we can at least find a readily integrable relation between a and e from division of equation (4) by equation (5). The result, after integration, is

$$a = \frac{C e^{4/5}}{1 - e^2}. \quad (8)$$

* Russell, Dugan, and Stewart, *Astronomy* (Boston: Ginn & Co., 1938), p. 534.

水星の近日点
移動の速度は
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さてこれより、水星の永年変化を見よう。近頃、前掲の式(7)を、水星の密度 ρ と、初期の距離 a と、初期の偏心率 e とから、水星の近日点移動の速度を求めよう。水星の密度 ρ は、 10^4 gm/cm³ とする。初期の距離 a は、 10^8 km とする。初期の偏心率 e は、 0.2 とする。

式(4)より、 $\frac{da}{dt} = \frac{2\alpha}{a} \frac{a^2}{1-e^2} = \frac{2\alpha}{a} \frac{a^2}{1-e^2}$ 。式(5)より、 $\frac{de}{dt} = \frac{2\alpha}{a} \frac{a^2}{1-e^2} \frac{e}{1-e^2}$ 。式(8)より、 $a = \frac{C e^{4/5}}{1-e^2}$ 。式(8)より、 $a = \frac{C e^{4/5}}{1-e^2}$ 。

$$t = \frac{a^2}{4\alpha} = 2.0 \times 10^6 s \rho a^2 \text{ years,} \quad (7)$$

さて、 t は、半径 s cm、密度 ρ gm/cm³ の粒子が、落下する全時間である。初期の距離 a は、 10^8 km とする。初期の偏心率 e は、 0.2 とする。式(8)より、 $a = \frac{C e^{4/5}}{1-e^2}$ 。式(8)より、 $a = \frac{C e^{4/5}}{1-e^2}$ 。

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$$\frac{de}{dt} = \frac{5\alpha e}{2a^2 (1-e^2)^{3/2}} = \frac{-5\alpha e}{2 \frac{C^2 e^{8/5}}{(1-e^2)^2} (1-e^2)^{3/2}} = \frac{-5\alpha (1-e^2)^{3/2}}{2 C^2 e^{3/5}}.$$

また、 $\alpha = \frac{3.55 \times 10^{-8}}{s \rho} \text{ au}^2/\text{years}$ 。式(7)より、 $t = \frac{a^2}{4\alpha} = 2.0 \times 10^6 s \rho a^2 \text{ years}$ 。

This relation is in contrast to the four-thirds power law found by Fessenkoff⁴ for the nonrelativistic solution. The constant in equation (8) will hold at all times for any given particle, and, if we know a_0 and e_0 at any arbitrary time, it can be computed, once and for all, by solving for C :

$$C = a_0 e_0^{-4/3} (1 - e_0^2). \quad (9)$$

この関係は、フェセンコフの相対論的解と見比べると、4/3 次法則と対照的である。
式(8)の定数 C は、粒子の位置と時刻 t を任意に選べば、 a_0 と e_0 がわかれば、 C は一定の値になる。
解の関数 C は、 a と e の関数である。

$$C = a_0 e_0^{-4/3} (1 - e_0^2) \quad (9)$$

From the earlier equations it is not possible to find a relation $a = a(t)$ that is independent of e . However, by substituting equation (8) in equation (5), one finds a relation involving only the eccentricity and time,

$$\frac{de}{dt} = -\frac{5a(1 - e^2)^{3/2}}{2C^2 e^{3/2}}.$$

Or

$$(t - t_0)_{\text{years}} = -\frac{2C^2}{5a} \int_{e_0}^e \frac{e^{3/2} de}{(1 - e^2)^{3/2}} = 1.13 \times 10^7 s \rho C^2 \int_{e_0}^e \frac{e^{3/2} de}{(1 - e^2)^{3/2}}, \quad e_0 > e, \quad (10)$$

where s and ρ are in c.g.s. units. The constant C^2 has the dimensions (A.U.)² and is evaluated from equation (9) by using the constants of the orbit. Then $(t - t_0)$ is given directly

TABLE 1
THE TIME INTEGRALS

e	$G(e_0)$	$(t - t_0)/10^7 s \rho q^2$ years	e	$G(e_0)$	$(t - t_0)/10^7 s \rho q^2$ years
0.00		0.704	0.78	0.771	4.10
.05	0.0052	0.778	.80	0.846	4.42
.10	.0158	0.858	.81	0.889	4.60
.15	.0305	0.946	.82	0.934	4.79
.20	.0489	1.04	.83	0.983	5.00
.25	.0710	1.15	.84	1.04	5.23
.30	.0969	1.27	.85	1.10	5.49
.35	.127	1.40	.86	1.16	5.77
.40	.162	1.55	.87	1.23	6.08
.45	.202	1.72	.88	1.32	6.43
.50	.249	1.92	.89	1.41	6.83
.55	.305	2.15	.90	1.51	7.29
.60	.370	2.42	.91	1.63	7.82
.62	.400	2.54	.92	1.78	8.45
.64	.432	2.68	.93	1.96	9.22
.66	.468	2.82	.94	2.17	10.17
.68	.506	2.98	.95	2.45	11.39
.70	.548	3.16	.96	2.82	13.06
.72	.595	3.36	.97	3.37	15.50
.74	.647	3.57	.98	4.30	19.60
0.76	0.705	3.82	0.99	6.37	28.89

in years. Although the integral cannot be found directly, the integrand is independent of the particle under consideration, and numerical integrations can be performed that will hold for all cases. We have tabulated in the second and fifth columns of Table 1 the function

$$G(e_0) = \int_0^{e_0} \frac{e^{3/2} de}{(1 - e^2)^{3/2}} \quad (11)$$

for interesting values of the eccentricity. Now, upon substitution of arbitrary particle radius, density, C^2 , and the quantity tabulated in Table 1 for some initial eccentricity,

⁴ A. J. Soviet Union, 23, 366, 1946.

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we can find the total time for the particle in question to spiral into the sun. For the time between any two nonzero eccentricities, one, of course, uses the difference between the corresponding tabular values.

件入アルゴニヨツテ 離る空ト時間ダケヲ 含ム 南條ヲ 見ツケレコトガ出来る

$$dt = -\frac{2x^2}{5x} \cdot \frac{e^{x/2}}{1 - e^{x/2}} dx \quad \text{de f'log}$$

$$(t - t_0)_{\text{years}} = -\frac{2c^2}{5\alpha} \int_e^{e_0} \frac{e^{3/5} de}{(1 - e^2)^{3/2}} = 1.13 \times 10^7 \text{ s} \int_e^{e_0} \frac{e^{3/5} de}{(1 - e^2)^{3/2}}, \quad e_0 > e, \quad (10)$$

$$(12) \quad \int_a^b f(x) dx = - \int_b^a f(x) dx$$

コデ STP の C.G.S 単位で表ワルヤル。定数 C^2 は $(AU)^2$, 次元ヲ持ツヤル, 軌道, 定義ヲ用イテ
(9) = ヲツテ 求メラル。 γ 27 $(\alpha - \alpha_0)$ 年デ表ワカル。

・ 複合の簡易には、ボルトンが、複合式は、今考へた粒子には、舞動像で、全の場合に、取り立つ、複合の、数値は、決り、
コが、第1の、 T_{400} 、2番目と5番目、本質に、 $e = \gamma$ 、イテ、

$$G(e_0) = \int_0^{e_0} \frac{e^{3/2} de}{(1 - e e_0)^{3/2}} \quad (11)$$

1 個が エネルギー、質量、半径、密度と C^2 と、初期値 = ツイテ Table 1 = エネルギー値を用いて
太陽 = ランダム、軌道を描いて落下する = 要する全体時間を知ることが出来る。セグメントの比率！ 2π / 進
1 周 = 要する時間。また、その時に必要な燃料、差を用いて知ることが出来る。

p. 137, 4行目

For total times of fall to the sun from any initial eccentricity in terms of particle radius, density, and perihelion distance, the calculation can be made far simpler, although less general, by a reduction of equation (10). From equation (8), since

$$q = a(1 - e),$$

we find

$$C^2 = q^2 (1 + e)^2 e^{-8/5}, \quad (12)$$

And thus, for total time of fall to the sun,

$$(t-t_0)_{\text{years}} = 10^7 s \rho q^2 \left[\frac{1.13 (1 + e_0)^2}{e_0^{3/2}} \int_0^{e_0} \frac{e^{3/2} d e}{(1 - e^2)^{3/2}} \right]. \quad (13)$$

We give in Table 1, third and sixth columns, the bracketed quantity in equation (13). For numerical results it is now required only to substitute for s and ρ in c.g.s. units and q in astronomical units. The latter quantity is directly available in most cometary and meteoric catalogues. It should be noted, however, that these results hold only for total time of spiraling into the sun and that the second and fifth columns of Table I should be used for the times between two arbitrary eccentricities.

最初、離心率/値が、太陽=落下 200° 、全時間=7分、光子、半徑、密度と近接距離=30リテ、F=一般の
F=1が、式(1)の改定計算の簡単=スカラー計算、式(2)が、 $f=a(1-e)$ F=1から

$$C^2 = g^2(1+e)^2 e^{-8/5} \quad (12)$$

 $t + 12$

(2) $f = a(1-e)$ $\Rightarrow a = f(1-e)^{-1}$, $1-e^2 = (1+e)(1-e) \neq 0 \Rightarrow (1-e^2)^2 = (1+e)^2(1-e)^2$
 $\Rightarrow (2) \Rightarrow c^2 = a^2 e^{-\frac{8}{5}} (1-e)^2 = f^2 (1-e)^2 \cdot e^{-\frac{8}{5}} (1+e)^2 (1-e)^2 = f^2 (1+e)^2 e^{-\frac{8}{5}}$ (12)

$$C(2) \cap C^2 \cap (10) = \emptyset \quad \lambda \geq 14$$

$$(t - t_0)_{\text{years}} = 10^7 \text{ s} \cdot \text{yr}^2 \left[\frac{1.13(1+e)^2}{e^{95}} \int_0^{e_0} \frac{e^{35} \cdot de}{(1-e^2)^{3/2}} \right]. \quad (13)$$

 $t + iv$

Table 1, 3番目と6番目: 本欄 = 式(13), オココ[] 中1値ヲ示ス. 数値計算結果ハ STPヨCg.s
単位デ8ヲ天単位代メ入ルコトガ要ナレバ. 7/1後, 数値ハ, 9/10, 彗星ハ流星ノカクガ直線ニ
シテアル. シカシコレノ結果ハ太陽ニラセン時ニ落下スル時間ヲ示ス. Table 1, 才2ト才5本欄ハ, 2/1
任意ノ密度ニ差ニテ用イラレベキデアルコトヲ注意ス.

Using the general relations for $a = a(e)$ and $q = q(e)$ in equations (8) and (12) in combination with that for $e = e(t)$, it is a straightforward matter graphically to relate semi-major axis or perihelion distance directly to the time. A calculation of $a(t)$ for various known meteor orbits shows a reasonably linear decrease of semi-major axis with the time to a given point, which depends on the value of C for the orbit in question, but averages about 1 A.U. Then the decrease in a is accelerated, and finally the particle falls into the sun in very short order. A plot of $q(t)$ shows a very slow decrease over most of the time but finally, also, a fast drop into the sun. The curves in Figure 1 show the nature of these relations for the Giacobinid and Leonid meteor showers.

The application of these results to small particles is interesting. As has been pointed out, the operation of the Poynting-Robertson drag should have been effective in sweeping out rather large volumes of the solar system in astronomically short times. For example, in the slowest case, that of bodies in circular orbits, we find that all particles of density 4 gm/cm^3 , radius $\leq 1 \text{ cm}$ and initially within a sphere of radius of 1 A.U. centered on the sun, will fall into the sun in a period of 2.8×10^7 years.

式(8)ト(12)ノ一般形ト関係 $a = a(e)$ ト $q = q(e)$ ヲ用テ $e = e(t)$ ト合セテ, 軌道半長径ト近日距離ノ時間ト関係ヲグラフニ直線的ニ見ルコトヲ出ス. 既知ノ流星軌道, $a(t)$ ノ計算結果ハ, 軌道半長径ガ時間ト共ニ直線的ニ減小シテアルコトガワカル(Fig. 1). ソレハコレノ軌道ノCノ値ニ依リテ, 平均約1天文単位デアル. ソレハCノ減少ハ加速化サレテ最終的ニ粒子ハ太陽ニ大ハシ短時間ニ落下ス. $q(t)$ ノ表示ニヨリ, 9/10全時間ニワタテ大ハシユツク減小シテ最終的ニ, コレニテ速ク太陽ニ落下ス. 才1図ハ, ショウニ群トシテ群ノコレノ関係ノ性格ヲ示シテ.

ルヤイ微粒子ニコレノ結果ヲ適用スルコトハ興味アルコトデアル. 8/10指搦シ様ニP.R.ノ抵抗作用ハ, 太陽系内ノ比較的大キイ物体ヲ, 天文學的ニハ短時間ヲ掃出スルニ効果的デアル. 例ハ, 最も速イ場合デ, 円軌道ニアル物体ノ密度ガ 4 gm/cm^3 デ半径 $\leq 1 \text{ cm}$, 最初太陽ヲ中心スル半径1天文単位ノ球形ノ中ニアルモノハ, 太陽ニ 2.8×10^7 (2800万)年ノ時間ヲ要スルデアル.

$$(e=0.00 \text{ 才 } s=4, f=1, q=1 \text{ トシテ } 0.704 \times 4 \times 10^7 = 2.8 \times 10^7 \text{ 年})$$

We have selected several of the known meteor showers, and, using Yamamoto's⁵ elements for the parent-comets (except for the parentless Geminid shower, where we have used Whipple's⁶ elements for a photographed meteor), we have calculated the total time for these shower particles to fall into the sun. The results are shown in Table 2. The first four columns are self-explanatory; the fifth gives the constant C appearing in equation (8); the sixth gives the times of fall as computed from Table 1 in terms of particle radius and density; and the seventh gives, by way of comparison, the times as calculated from equation (7), assuming circular orbits. For example, a particle of radius 0.05 cm, corresponding to about a fifth-magnitude meteor, and of density 4 gm/cm^3 moving in the orbit of Halley's Comet would be drawn into the sun in about ten million years. It can be seen from the sixth column of Table 2 that the lifetimes of faint visual meteoric bodies in the well-known showers are relatively short astronomically.

17/10既知ノ流星群ヲ選ビ, 山本雅夫ノ彗星カクダノ母彗星(母彗星ガイヌ子座群ハ, ホイッフルノ宝真流星ノ軌道要素ヲ用テ以外ハ)ノ軌道要素ヲ用テ, コレノ流星群ノ粒子ガ太陽ニ落ルマデノ時間ヲ計算シ, 結果ハ Table 2ニ示ルデアル. 才14本欄ハ, 自ラデ理解スルコトガデキルダロウ. 才5本欄ハ, 式(8)ニアル定数Cデ, 6番目ハ粒子ノ半径ト密度ニヨリ才1表デ計算デキル落下時間ヲ示ス. 7番目ハ円軌道ト仮定シ, 式(7)ニヨリ計算デキル落下時間ヲ比較シテ示ス. 例ハ半径0.05cmノ, 1/10ニ対応スル光度ノ約5等デ, 密度ハ 4 gm/cm^3 (ハレー彗星)ノ軌道ヲ動シテアルモノハ約1000万デ太陽ニ落下ス. Table 2ノ才6番目ノ本欄カク, コノカク流星群ノ因明流星ノ寿命ガ天文學的ニ比較的短イコトガワカル.

(7)

8等(5等星)

We inquire now as to the possibility of observing the Poynting-Robertson effect during a meteor shower. From equation (10) it is evident that the times involved depend

¹ *Pub. Kwasan Obs.*, Vol. 1, No. 4, 1936.

⁴ *Proc. Amer. Phil. Soc.*, Vol. 91, No. 2, 1947.

注意群/期中中 = 只知效果ヲ観測スルコト出ル可能性ニツケ尋ナシ。式(10)カ
含マレテハ時制ハ種子ノ下ナリ密度ニ直接の(一次式/時係数)乘積ニテカノ明カデアル。
(10) (9)ノ判行ニツキテ。

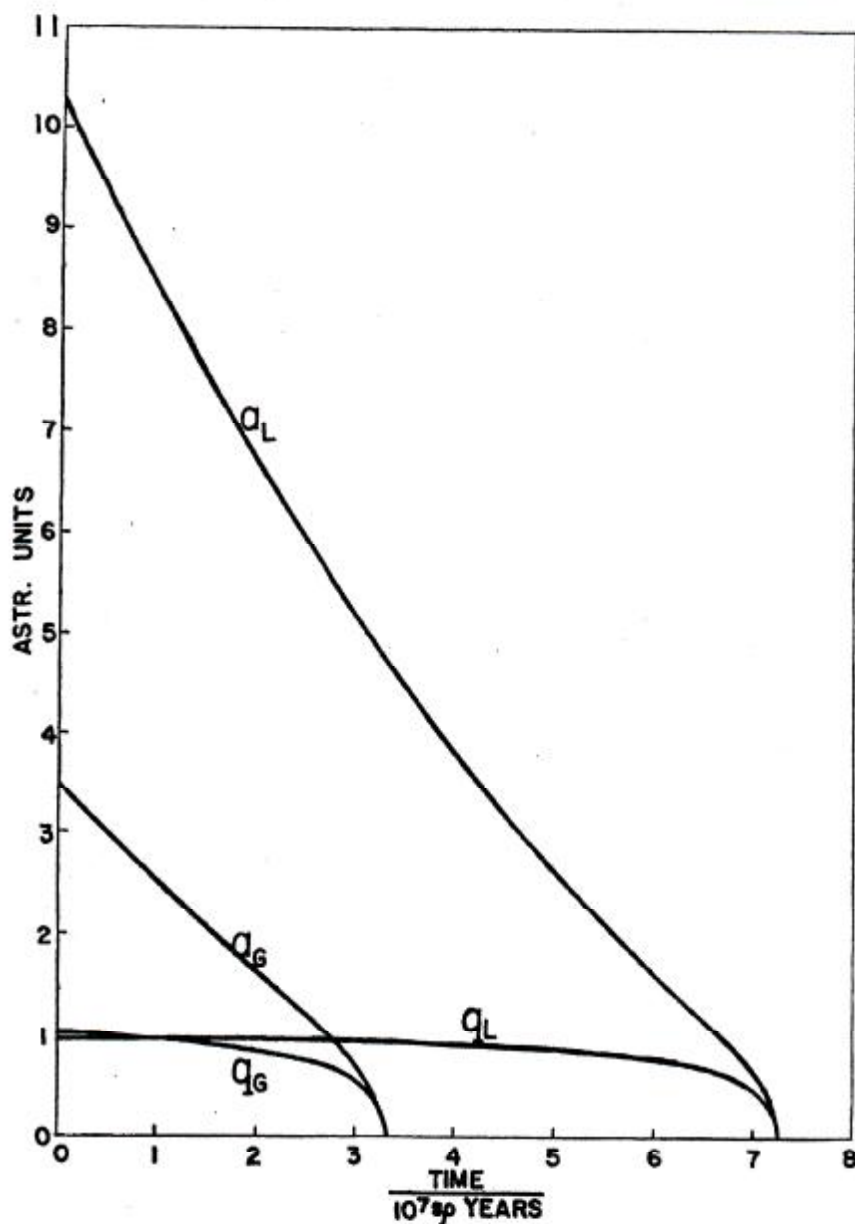


FIG. 1.—Semi-major axis and perihelion distance as functions of the time for two showers. Subscripts *L* refer to the Leonids and *G* to the Giacobinids. Times are reckoned from the present epoch.

判図 2y, 遠望群 = Y 分 時刻/度数/計, 半長径軸上 近距離巨離。添字, L n 山主群
 G n 2nd = 群マボス 暗部 (Time) n 理存在 測(メ)テリ
 (Tab 2 = 300 C- $\times 10^3$ g n L : 2.24 Glacobioids: 3.32, d n L : 10.325, G : 3.520)

(9)

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linearly on the particle size and density. Let us make the simplifying assumptions, first, that the density of every meteoric particle is 4 gm/cm^3 and, second, that a meteor shower originates as a uniformly dense swarm occupying an elliptical orbit with small circular cross-section in the plane normal to the velocity vector of the particles. If there is dispersion in the individual meteor radii, the smaller ones will be drawn toward the sun far faster than will their larger neighbors. At some time later, the cross-section of the swarm will be elongated in the radial direction relative to the sun, with the smaller particles orbiting closer to the sun. The conditions for observing this effect on earth are that the inclination of the shower shall be moderately low or retrograde and that enough time shall have elapsed since the formation of the shower for the various-sized particles to have been separated sufficiently for detection.

仮定する簡単ニシテコウ。初メニ流星群ノ密度ヲ 4 gm/cm^3 2番目ニ、流星群ハ、粒子ノ運動速度ニ
 ナンテ垂直ノ平面内ニハサイ円形ノ断面ヲ持テ、楕円軌道ニ上ニ一様ニアル密度ノ流星
 群ヲ成シテイルモトスル。モシ個々ノ流星群ノ値ガ分散シタルハ、ハサイモハ、 γ
 近クニアルハキモ、シリ早ク太陽ニ引ッハラル。ソレヲ後ニハ流星群ノ断面ハ太陽ニ面シ
 高徑ノ方向ニ伸ビレダロウ。ハサイ粒子ノハサイモヨリ太陽ノ近クニ運動スルコトナリ。地球ガ
 コノ如キヲ観測スル条件ハ、流星群ノ軌道傾斜角ハ、ヤヤ低クナルマデハ進行スル様ニ
 ナリ、 γ ハハハキサノ粒子ガ、軌道傾斜角ノ大ニ分高ニスル様ニナルハ、流星群ガ全クシ
 テカラ完全ノ時間ガ経過シタルハナリ。

As an approximation to the orders of time involved in separating bright and faint particles for observation, we take all the above-listed showers with $i < 40^\circ$ and assume

TABLE 2
TIMES OF FALL FOR SHOWER PARTICLES (流星群ハ太陽ニ面シタル時ノ時間)

Shower	Parent-Comet	a	e	C	$(t-t_0)/10^3 \text{ yr}$	$(t-t_0)_{\text{obs}}/10^3 \text{ yr}$
Geminids.....	1.396	0.900	0.289	0.143	1.4
Taurids.....	Encke	2.210	.8498	0.6995	0.605	3.4
Bielids.....	1852 III	3.5259	.75592	1.8902	2.79	8.7
Giacobinids.....	1933 III	3.520	.7160	2.241	3.32	8.7
Orionids?.....	Halley	17.96	.9673	1.186	5.10	230
Leonids.....	1866 I	10.325	.90542	2.0145	7.24	75
Perseids.....	1862 III	24.277	.96035	1.9491	12.2	410
Lyrids.....	1861 I	55.665	0.98346	1.8508	18.6	2200

TABLE 3
TIMES OF SEPARATION (分離スル時間)

Shower	Years	Shower	Years
Geminids.....	7×10^4	Bielids.....	2×10^6
Taurids.....	5×10^6	Leonids.....	3×10^6
Giacobinids.....	1×10^6	Orionids?.....	5×10^6

that all $i = 0^\circ$, that the earth's orbit is circular, and that the perihelion advance of the shower is of no consequence. We now inquire how long it will take to separate fifth-magnitude meteors from those of magnitude -2 , so that the earth will pass from one limit to the other in a period of 5 days. It should then be possible to observe a gradually changing mean magnitude over the period. The radii of such meteors are calculated separately for each shower. We take, as before, a density of 4 gm/cm^3 . We then apply to Watson's⁷ values of mass, which were computed for meteors with velocity of 55 km/sec , a correction for the actual observed shower velocities listed by him.⁸

明メ、ハ暗イ粒子ノ分離ガ観測デキル様ニナルゲタノ時間ノ大キサヲ近似即ニ地球外ニ上列ノ $i < 40^\circ$
 ノ流星群ノ、 γ ヲ $\gamma = 0^\circ$ ト仮定シテ、地球軌道ノ円 ($e=0$) トシ、近点ノ前進ハ考ヘ
 ナルコトナリ。光度 -2 ト 5 等ノ流星ガ分離ガ経ッテ地球ガコレノ限界ヲ5日ガ内デ通り
 テル様ニナル時間ヲ求メテ、 $\rightarrow (10)$

(9)

⊕ This correction factor is calculated on the assumption that the kinetic energy of a meteor is proportional to its luminosity. The steps in the geometrical approximation applied are to solve for the present true anomaly of the intersection of earth and shower, to increase this by 5° , to find by equation (8) the new a and e satisfying the new true anomaly, and to integrate between the old and new eccentricities to determine the time. The results indicate the correct order of magnitude for the times of separation and are given in Table 3. Definitive correlations → p. 140

⁷ *Between the Planets* (Philadelphia: Blakiston Co., 1941), p. 115.

⁸ *Ibid.*, p. 123.

→ (9) / 丁カ 5行目カ、

コノ範囲中ニ流星、平均光度ガユツクリ変フレハ、ユヲ観測スル可能性ガアルニ違イナイ。
コノ母+流星ノ半径ハ、ルツレノ流星群ニゴトニ計算スル。先ト同様ニ密度ヲ 49gm/cm^3
トスル。質量ハワトソン Watsonノ値ヲ採用スル。ルツハ流星速度ヲ 55km/sec トシテ
計算スル。距離ノ速度補正ハ後ニ述ベテリストアルデイル (ケト8ノ注ヲ参照スルコト)。

(*) コノ補正係数ハ流星ノ力学エネルギーハ明セニ比例スルノ一定ニ述ベテ計算アルデイル
適用ナレバ幾何学的近似ノ過程ハ地球ト流星群ノ交差スル長ノ真近距離ヲ求メルヤニ式(8)ニヨリテ
新シイ真近距離ヲ算出スル。アルトニ述ベタルヤニ50ツツ増カスルヲ算デアル。ソレヲ時間ヲ決メ
ルヤニ新シイ真近距離ノ向隔ニソレヲ積分スルコトデアリ。コノ結果ハ全時間ノ正シ大サ
ヲ示シテ、Table 3ニ示サレイル。

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of magnitude and time apparently are not found in observations of meteor showers. A shower may be of very recent origin so that the particles have not had time to become separated radially. Such may be the case with the Giacobinids. Among the older showers, where the magnitude effect should appear, those with orbits of low inclination and therefore favorable for observation of the effect are also most seriously affected by planetary perturbations. Since these perturbations are nonselective with respect to particle size but may be capable of dispersing the showers, the times given in Table 3 must be considered only as upper limits to the possible ages of the showers. It may be possible in the near future, by combining extensive data from visual, photographic, and electronic observations of meteor showers, to detect a systematic effect of the sort that we have outlined above.

光度ト時間トノ関係ヲ相関トスルハ流星群ノ観測デハハツキトイ見ツクナリ。流星群ハ恐ラク
マシ最近ニ生シタマデアロウ。然レテ流星ガ動径方向ニ分散スル程ニアル時間ヲ持
ツテイナイタク。何故射撃ニトベキカ？コレハジャコビニ群ノ場合ガソノ持テイル。
古い群ノ中デハ、光度効果ガ表サレイル等ノ群デハ傾斜角ガ低ク、コノ効果ヲ観測スル
ニハ有利デアリガ、ソレハ流星群ニヨリテオカク影響アルデイル。コレノ観測ハ流星群
ノ大サニハ相関係デ流星群ヲ分散セルコトガ出来ナイ。Table 3ニ示サレイル時間ハ
流星群ノ可能ノ寿命ノ上限トイフベキデアリ。上ニ述ベタル系統ノ効果ノイロイ
ロヲ、暗視ヤ、写真、電波観測ト多クノデータヲ組合セテ検出スルコトガ、近い将来可能ニアル
ゾロウ。

Although meteor showers have in nearly all cases been identified with comets, the origin of sporadic meteors is not so clear. It is possible that some sporadic meteors have a common origin with the meteorites, which Harrison Brown and Claire Patterson⁹ have shown to be planetary debris. It seems justified to make the unproved assumption that meteorites and asteroids are associated generically. Since the mean semi-major axis for the known asteroids is about 3 A.U., we may assume, in addition, that the parent-planet (or planets) of the meteorites disintegrated at about this distance from the sun. Particles

R140, Fが3行目。太陽系ノ外ノ区域デ、P.R.効果ヲ考ヘル場合ニハ、与ヘラレタ軌道ヲ持ツ天体ノ時間ヲ考ヘルニハ、太陽ノ周リ、軌道ト同ジ軌道ヲ持ツ巨シ大キナ物体ニ、太陽カ交角ナル1秒間アリ全エネルギート物体ニコソテ放射サセレエネルギート、比、 E_0/E ヲ係数トシテ乗ズルレバ同じコトナリ

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and emitted by the sun to that emitted by the parent-star. In order to utilize the results given above, we must, of course, continue to express a and q in astronomical units. Near the large and hot B stars the times will be shorter than those near the sun by a factor of about 100,000, whereas for particles near M dwarfs the times will run approximately one hundred times as long.

上ニ与ヘラレタ結果ヲ用化外ニハ、 E_0/E ノ値ヲ天文単位デ表シテ、用イ概ク+2.0ニナリ。大キテ巨シB型星ノ近クデハ、落下時間ハ、約100,000割合デ太陽ノ近ク場合ヨモ短クナル。M型星ノ近クノ粒子ニサレハ、サラニ100倍グナイ、近似的ニ長クナル。

The nucleus of the galaxy gives a negligibly small effect on the orbits of interstellar particles. What effect there is depends markedly on the co-ordinates of the particle concerned, since the net radiative flux vector due to the Milky Way will vary in magnitude and direction at each point of space because of the irregular distribution of bright clusters and overlying dark clouds. However, even for an idealized unobscured galaxy of absolute magnitude -15 and radius 1000 parsecs, where E_0/E may be taken as about 10^{-8} , it is found that the time to spiral into the nucleus for a body of $sp \leq 4$ is 10^{16} years for an initially circular orbit. And, although for highly eccentric orbits the times may be less by a factor of, say, 100, it is clear that the Poynting-Robertson effect has been of very little significance galactically. Its importance is restricted to small particles orbiting in the vicinity of individual stars.

銀河ノ中心核リ、星間空間ニ^(粒子)P.R.効果ニ対シテハ、近視出来クナイ、ホサイ効果シカ与ナリ。粒子ノ座標ニコソテ、 E_0/E ノ値ヲ天文単位デ表シテ、用イ概ク+2.0ニナリ。大キテ巨シB型星ノ近クデハ、落下時間ハ、約100,000割合デ太陽ノ近ク場合ヨモ短クナル。M型星ノ近クノ粒子ニサレハ、サラニ100倍グナイ、近似的ニ長クナル。

Lurgi G. Jacchia 1951. 3. ヤキア
in The Solar System III, Meteors, Meteorites, and Comets
pp. 783-785.

p. 783 33. The Yarkovskii - Radzievsky Effect
ヤロフスキ-ラヂエフスキ効果

ヤロフスキ-ラヂエフスキ効果は、重力で動いてる粒子はコップの吸盤の太端にエネルギーが動いてる方向に一樣に再放射されて位置がシフト、しかし粒子が回転して、吸盤の方向に放射方向に差が出来る、この差は粒子の自転角速度に左右される。その粒子の大きさと熱伝導率に比例する、この差の結果、横方向に力が生じ、これがP.R.効果と同じ効果に働き、自転と軌道運動が反対方向で進む、この力ハ彗星(P.R.効果)に比べると倍は働か、もし自転と軌道運動が同方向で進む差は半分の働き、この効果ハ、エック(1951)とLovell(1954, p. 410)が見出し、1950年ごろ Yarkovskii = エックが提議した。1952年 = ラヂエフスキが、ヤロフスキとエックの論文を知らずに独立に同じ効果を見つけ、エックの本質的 = 同じ結論にたどり着いた。結論ハ次の通りである、この効果ハ粒子の回転周期 / 平方根 = 比例する、小惑星や隕石には重要であり、普通、隕石と同じ大きさの粒子では無視できる、しかしこの効果ハ、彗星、小惑星、小惑星の破片ハより大きくなる、自転周期が短く、この短周期(?) 若くは彗星破片ハ適用される、衝突理論に基づいて、ラヂエフスキ(1954)ハ、彗星の論文で、太陽系 / 小惑星 / 自転ハ放射圧 = エックが提議したコトを知り、議論ハ次の通りである、要するに反射される物質ハより放射圧 / 結果として(バックの放射方向)ハ、慣性力 / 中心を通り、そしてこのトルク(ネジ)は回転を生じ出す、後ハこの効果が小惑星や隕石の破壊スロウ = 効果的 = 作用する、大ハ重要 + コトが示さる、しかし、惑星の + 惑星が惑星の空間 = 自在な、それハ鉄磁性の粒子 / 回転の簡単 = 遅く、それハ何カを指摘してオカシな事、普通、流星微粒子 / 回転周期ハ0.1 ~ 1秒、程度で、これがヤロフスキ-ラヂエフスキ効果を、予想のモット重要 + モノ = シフトする、それハ + 示す、それハ + 示す。

(注)

3.4 Corpuscular, 粒体。太陽系内の粒子、影響ヤ

3.5 他、惑星物質、影響の事ハ + 示す、それハ + 示す

それハ、詳細ハ + 示す、それハ + 示す。